



*Rensselaer Polytechnic Institute
Mechatronics Research Program*

Identification of Backlash, Friction and Compliance in Machine Tool Drive Trains

National Science Foundation
Mechatronics in Machine Tools Grant

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Motivation

- **Drive nonlinearities cause machining errors**

- cause of positioning error in workpiece cutting and
- exacerbated when machining at high speeds and cutting
- cause of damage to workpiece and cutting tools

- **Frictional errors**

- thermal expansion
- stick-slip friction (stiction)

- **Back**

- tol
- im
- pit

- **Compliance error**

- vibration
- energy storage and release



Objectives

- Using a generalized model of drive nonlinearities, systems may be controlled more precisely and accurately
 - model nonlinear friction, backlash and compliance
 - model dynamic interaction between the components
 - apply model to, and verify using data from actual

• Friction model

• Compliance model

• Backlash model

• Complex dynamic



Overall Approach

- Develop analytical model
 - model nonlinear friction, backlash & compliance
- Develop system identification
 - verify system ID procedure on simulation
- Identify machine tool dynamics
 - test system ID on test bed and actual machine
 - corroborate known parameter values and procedure



Technical Details: Friction

- Static phenomena

- normal friction
(increases with normal load)
- rising friction
(increases with static contact time)

- Hysteretic

- presliding
(hysteretic)
- frictional
(hysteretic)

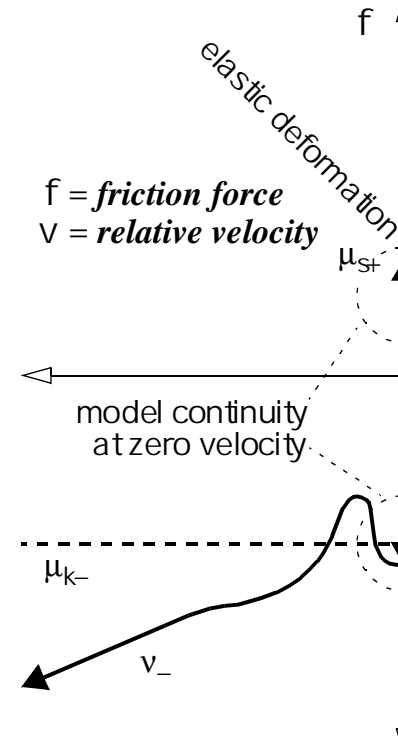
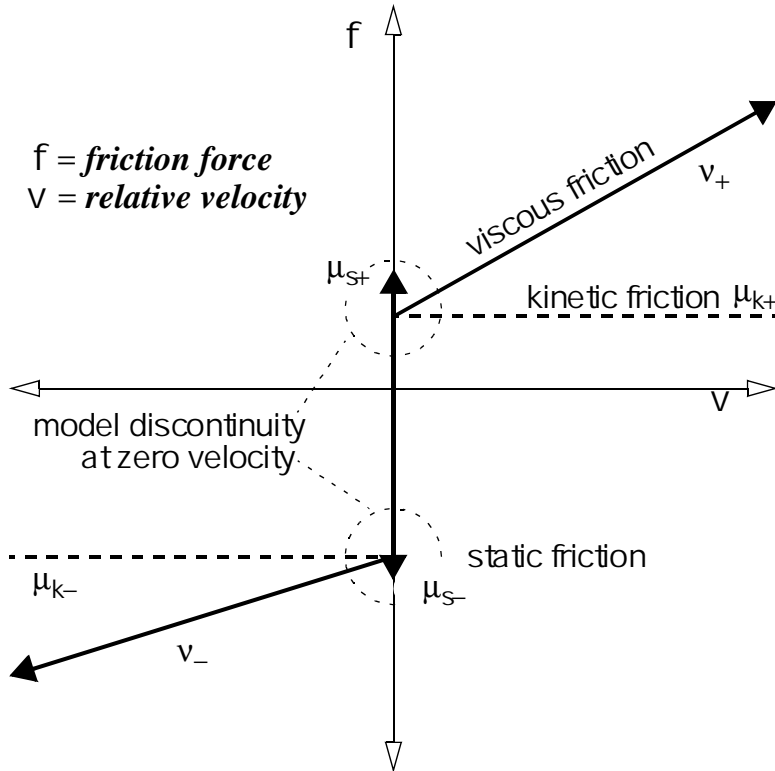
- Nonlinear friction

- Dynamic phenomena

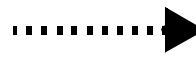
- Stribeck friction
(describes transition from static to kinetic)



Technical Details: Friction



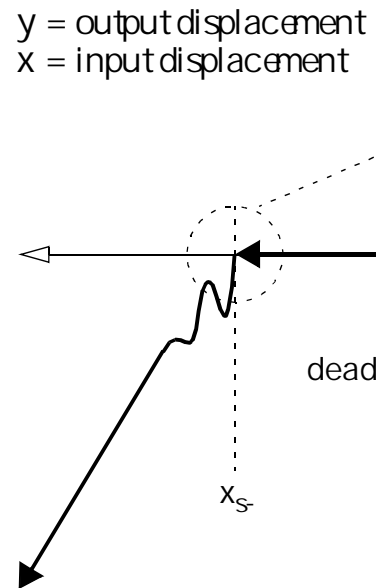
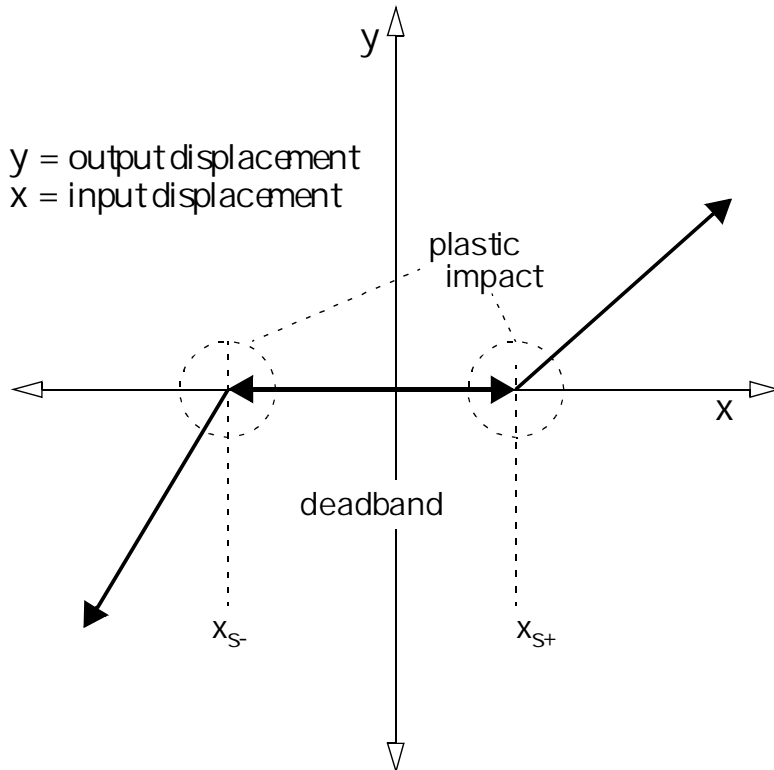
- Traditional model
 - discontinuity from static to kinetic



- Modern model
 - captures the dynamic friction and low velocity



Technical Details: Backlash

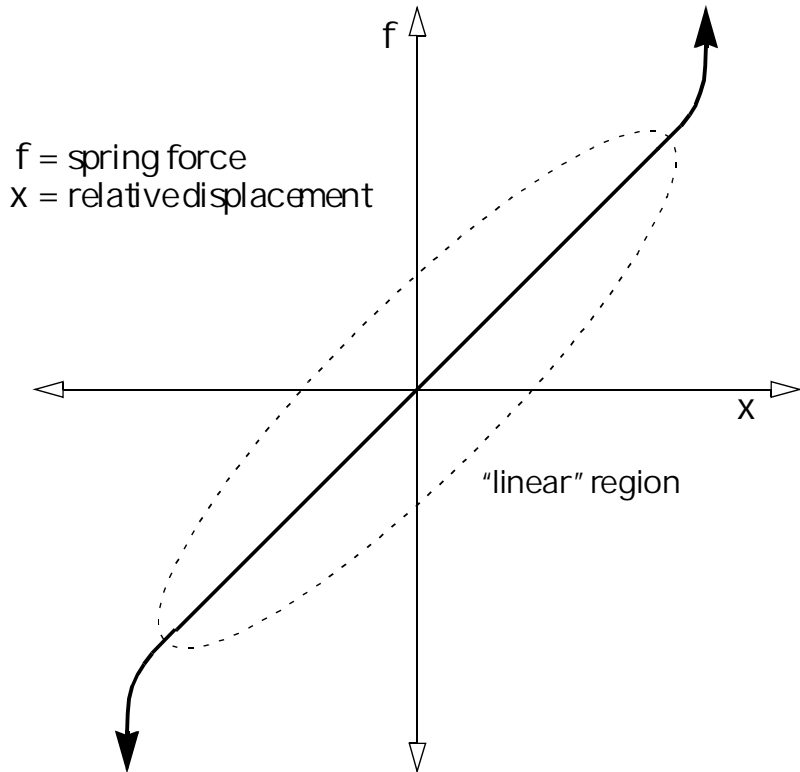


- Traditional model →
 - the backlash has no dynamic component

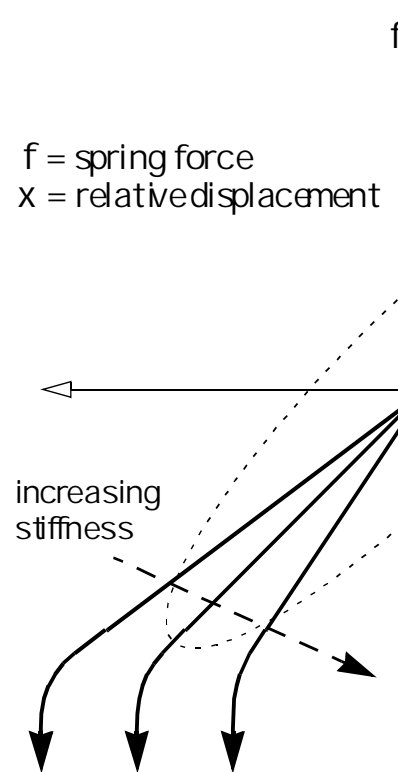
- Modern model (M)
 - impact-induced y included in the y



Technical Details: Comp



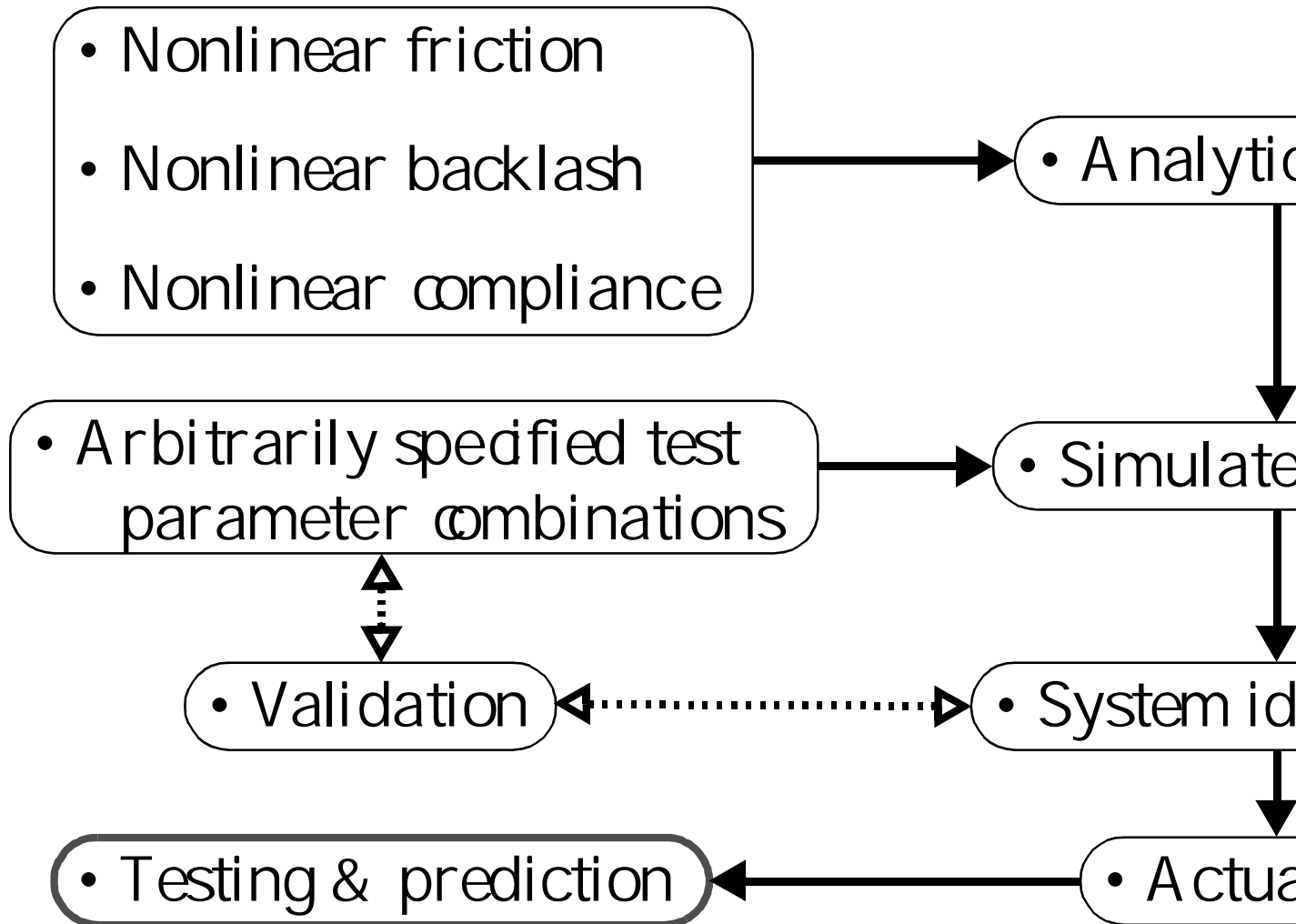
- Traditional model →
 - spring force is unimodal and linear



- Modern model
 - multiple modes spring forces a



Technical Details: ID Pro





Technical Details: ID Me

- Pros: Logarithmic decrement method
 - static, kinetic, and viscous friction
 - linear compliance
- Cons
 - req
 - piec
- Pros: Hilbert Transform
 - kinetic and viscous friction
 - unimodal nonlinear compliance
 - backlash with impact
- Cons
 - req
 - sim
 - fur
 - no

- Pros: Wavelet Transform
 - multimodal nonlinear compliance
 - cleaner data than Hilbert Transform

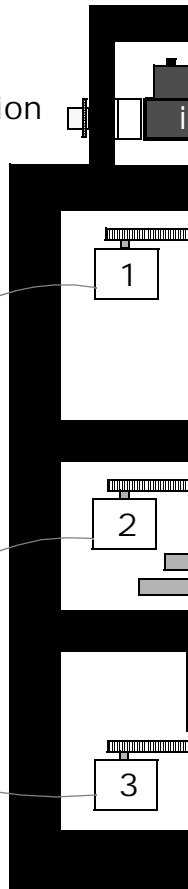


Results: Test Bed

- Unique test bed built for experimentation & validation
 - friction, backlash & compliance are arbitrarily adjustable
 - can mimick various actual machines and scenarios
 - one of only two in the U.S.

optical encoders

dry friction





Results: Objectives Achieved

- Modeling

- analytical models of nonlinear subsystems developed
- analytical model of fully-coupled subsystems in simulation

- System ID

- traditional methods extended to piecewise linear systems
- nonlinear Hilbert method verified on friction

- Actual machine dynamics

- system ID techniques corroborate published parameters



Results: Friction ID Exa

- System without
 - Coulomb friction
 - viscous friction
 - frictional bias
 - compliance
- Excited via the
 - harmonic oscillation
 - free vibration
 - logarithmic
 - Hilbert Transform
 - dual analyses
 - also provide



Results: Experimental

- Log decrement method
 - estimates compliance, Coulomb friction and bias
- Hilbert Transform
 - estimates friction, also can estimate



Unique Contribution

- **New** dynamic backlash model
 - state-of-the-art backlash model augmented to include
- **New** dynamic model & simulation of drive nonlinearity
 - fully nonlinear, coupled equations-of-motion
 - simulation of arbitrary friction, backlash & compliance
- **New** parametric harmonic oscillation ID
 - experimental method using P+D feedback to achieve desired vibration response in overdamped systems
 - machine resonance frequencies automatically eschewed
 - method allows use of log decrement, Hilbert and wavelet analysis without requiring a sine-swept forced harmonic oscillation
 - produces estimates of inertia and mass-based system parameters



Continuing Work

- Identification

- backlash
- backlash with compliance
- asymmetric (direction-dependent) nonlinearity
- periodic friction
- static and hysteretic friction

- Analysis

- extension to Wavelet Transform analysis

- Application

- automation of identification procedure



Future Work

- Application

- apply testbed results to an actual machine tool
- motorised workpiece table on drill press in laboratory

- Extension

- on-line and adaptive system ID techniques

- Development

- feedforward control and adaptive control



Lab Demonstration

- Nonlinear system modeling and simulation
- Signal processing details
- Mechatronic implementation
- Friction identification
- Backlash identification
- Compliance identification
- Machine tool instrumentation approach